

**Laser Physics I (PHYC/ECE 464)**

*FALL 2021*



*Midterm Exam, Closed Book, Closed Notes*

*Time: 4:00 – 6:00 pm*

NAME .....  
*last* ..... *first*

Score
-------

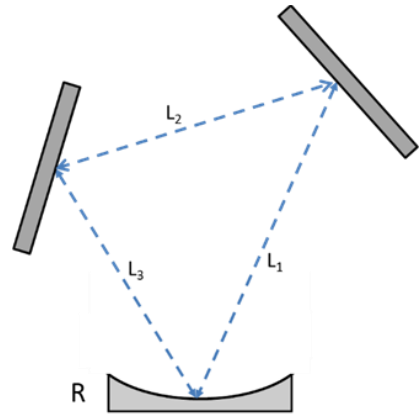
***Total= 100 points***

*Please staple and return these pages with your exam.*

*Instructor: M. Sheik-Bahae*

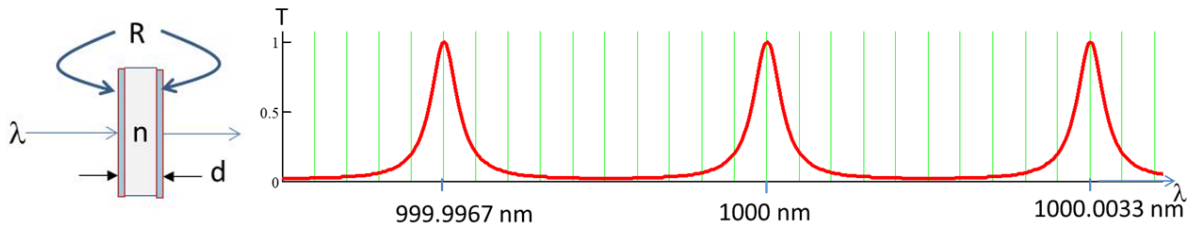
1. (25 points)

- (a) Using the ABCD matrix for a roundtrip, derive the stability condition for the ring cavity above in terms of  $d/R$  (with  $d=L_1+L_2+L_3$ ) (ignore astigmatism). (13pts.)



- (b) Obtain the position and the magnitude of the minimum beam waist  $w_0$  assuming a wavelength  $\lambda$ . (12pts.)

2. (25 points) Drawn to scale on the graph below is the relative power transmission of a tunable light source at normal incidence through a Fabry-Perot etalon as the wavelength  $\lambda$  is varied. The etalon is made from of glass having index  $n=1.515$  and thickness  $d$  with both sides mirrored with reflectivity  $R$ .

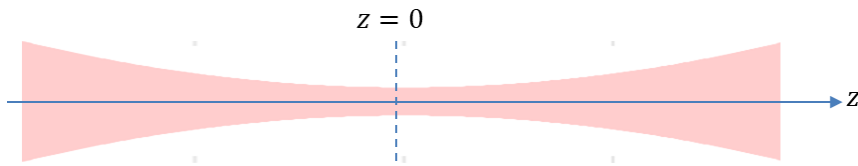


a. What is  $d$ ? (8 points)

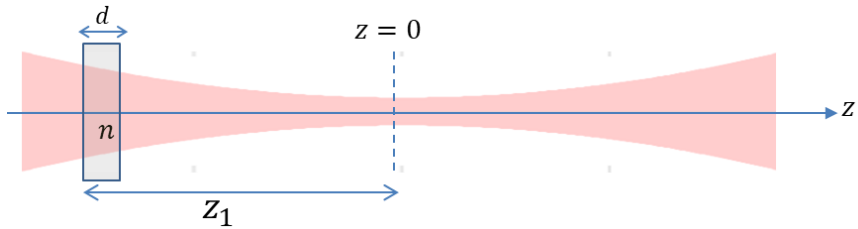
b. What is the *estimated Finesse* and the reflectivity  $R$ ? (7 points)

c. Draw (on top of the above graph) the transmission for the case where  $R$  is purely due to the Fresnel reflectivities at normal incidence (i.e. no coating). What is the *finesse* and the *minimum transmission* in this case? (10 points)

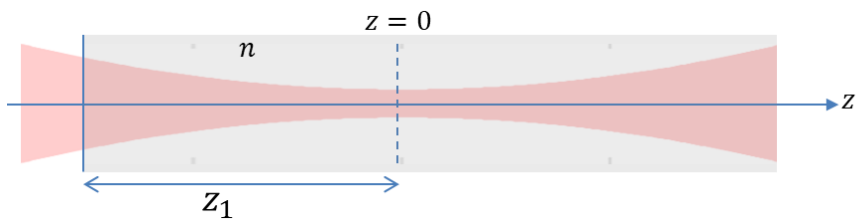
3. (25 points) Consider a fundamental Gaussian beam with known  $Z_0$  and wavelength  $\lambda_0$  travelling from left to right, as shown below.



(a) A glass window of thickness  $d$  and index of refraction  $n$  is inserted at a distance  $z_1$  prior to  $z=0$  (focus) plane as shown. Derive the distance ( $\Delta z$ ) and the direction (*sign*) by which the new focal point shifts. What is the new  $z_0$  (does it change at all)?



(b) Repeat part (a) for the case when the original Gaussian beam enters a material of index  $n$  with infinite thickness- as shown below.



4. (25 points) A two-level medium solid-state laser with the following property:

- Spontaneous emission lifetime:  $\tau_{sp}=1\text{ ms}$
- Homogeneous linewidth  $\Delta\nu_h=1.0\text{ THz}$
- Line center wavelength:  $\lambda_0=1\text{ }\mu\text{m}$
- Density of active ions (concentration):  $N_{total}=2\times 10^{19}\text{ cm}^{-3}$
- Non-degeneracy factors:  $g_1=8, g_2=6$

(a) What is the absorption coefficient  $\alpha(\text{cm}^{-1})$  at the line center ( $1\text{ }\mu\text{m}$ ) when all the molecules are in their ground state (level 1)? (15 points)

(b) What fraction of the molecules needs to be excited into level 2 in order to make this gas transparent (i.e. the onset of gain) at  $1\text{ }\mu\text{m}$ ? (10 points)