

NONLINEAR OPTICS (PHYC/ECE 568)

Fall 2017 - Instructor: M. Sheik-Bahae

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Homework #2, Due Wed. Sept 27

Problem 1. Infrared Up-Conversion

Estimate the efficiency of the upconversion of 10 μm infrared radiation using sum frequency generation. The pump laser has $\lambda=532\text{ nm}$, with a power of 10 W. Use 2 cm long proustite (use $d_{\text{eff}}=d_{22}$) crystal under perfect phase-matching and optimum focusing ($L=2Z_0$).

Problem 2.

(a) Show that d_{eff} , as defined by $P_3 = 4d_{\text{eff}} E_1 E_2$, is related to the d tensor via:

$$d_{\text{eff}} = \hat{e}_3 \cdot d : \hat{e}_1 \hat{e}_2$$

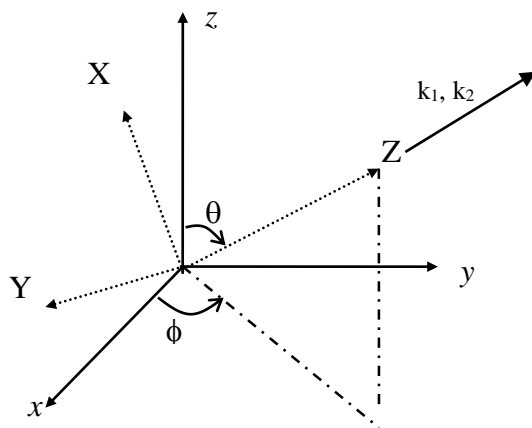
where \hat{e}_j ($j=1,2,3$) is the unit vector associated with E_1, E_2 , and P_3 .

(b) For a given geometry, d_{eff} is usually calculated in terms of d_{ij} 's and the angles ϕ and θ as described in the figure below. Here x, y and z (or $1, 2$ and 3) are the crystal axis and X, Y , and Z (laboratory frame) are optical propagation axis (e.g. $k_2 \parallel k_1 \parallel Z$). Note: Y is in xy -plane (thus normal to z - or optics axis) and X is on zZ plane.

(i) Derive expressions for d_{eff} for a class 3m crystal (e.g. LiNbO_3) where $\hat{e}_1 = \hat{e}_2 = Y$, and $\hat{e}_3 = X$. (As we will see later on, this is called type-I condition).

(ii) Repeat the above calculation for type-II condition where $\hat{e}_1 = Y$, $\hat{e}_2 = X$ and $\hat{e}_3 = X$.

(iii) Find a geometry (i.e. θ and ϕ) that accesses the largest d_{ij} element in LiNbO_3 . (see data provided here).



(iv) Find the phase matching angle for SHG generation at λ (fundamental)=1.15 μm for the part (i) and (ii). Discuss the phase matching situation for case (iii)

Problem 3. *Poynting Vector Walk-off:*

We know, from linear optics, that the e- and o-rays in a birefringent crystal walk-off from each other (i.e. double-refraction). In the harmonic generation applications, such as SHG, this imposes a serious restriction on the useful length of the nonlinear crystal.

- a. Assuming a uniaxial crystal, calculate the walk-off angle ρ between e- and o-ray Poynting vectors.
- b. Show that for type-I phase matching (o+o \rightarrow e)

$$\rho \approx \tan \rho = \frac{n_o^2(\omega)}{2} \left[\frac{1}{n_e^2(2\omega)} - \frac{1}{n_o^2(2\omega)} \right] \sin(2\theta_m)$$

LiNbO₃ Properties

$$\begin{bmatrix} 0 & 0 & 0 & 0 & d_{31} & -d_{22} \\ -d_{22} & d_{22} & 0 & d_{31} & 0 & 0 \\ d_{31} & d_{31} & d_{33} & 0 & 0 & 0 \end{bmatrix} \text{ class } 3m \text{ crystal}$$

Nonlinear Optical Coefficients at 1.06 μm (* $d_{31}=d_{15}$)

$d_{22} / d_{36}^{\text{KDP}} $	6.5
$d_{31} / d_{36}^{\text{KDP}} $	-12.3
$d_{33} / d_{36}^{\text{KDP}} $	-86

Refractive Indices at 20°C

Wavelength, μm	n_o	n_e
0.43584	2.39276	2.29278
0.54608	2.31657	2.22816
0.63282	2.28647	2.20240
1.1523	2.2273	2.1515
3.3913	2.1451	2.0822